

## USING THE Z-TABLE

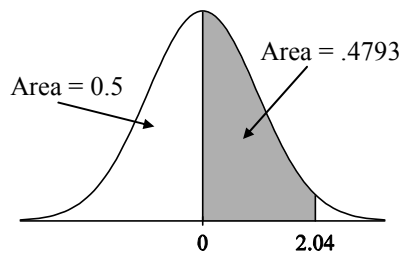
Learning to use the table of the standard normal distribution is extremely important! Make sure you can do problems like these without difficulty. Note that the total area under the normal curve is 1.000, with 0.500 in each half. At the middle line,  $z = 0$ ; to the right  $z$  is positive; to the left  $z$  is negative.

**Probability (or proportion or percentage) = area under the curve.** Start with your  $z$ -value, along the borders of the table, and look for area on the inside of the table.

**To find a  $z$ -value for a given probability or percentage (area):** Find the area on the inside of the table, and then read the  $z$ -value along the borders of the table.

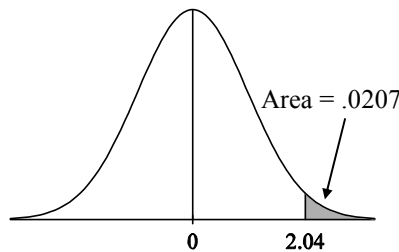
Your text uses two tables. One is a left-hand tail area and the other is a cumulative table extending from left to right. Because the distribution is symmetric, you can use the left-hand tail table to find an area in the right-hand tail – the  $z$  scores will be negative, but the area is the same – area is always positive!

**Find  $P(0 \leq z \leq 2.04)$**



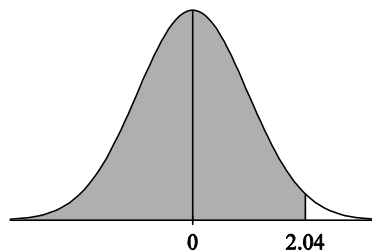
Look up *cumulative* area in the table and subtract 0.5000 from it.  
**Probability = .9793 – .5000 = .4793**

**Find  $P(z \geq 2.04)$**



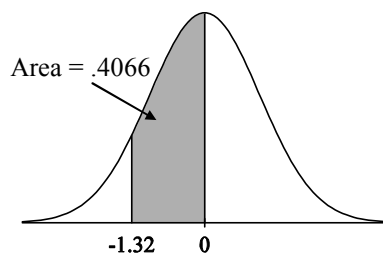
Look up the *cumulative* area in the table and subtract it from 1.0000. This is the area to the right of 2.04.  
**Probability = 1.000 – .9793 = .0207**

**Find  $P(z \leq 2.04)$**



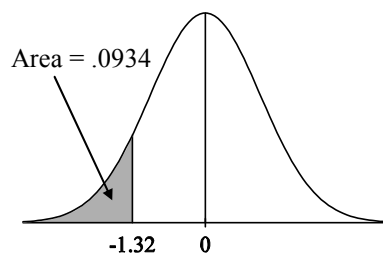
Read the area directly from the *cumulative* table.  
**Probability = .9793**

Find  $P(-1.32 \leq z \leq 0)$



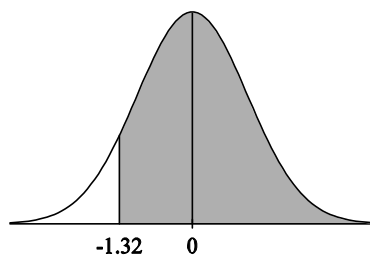
The total area to the left of 0 is 0.5. Look up the *tail area* to the left of -1.32 and subtract it from 0.5000.  
**Probability =  $0.5 - .0934 = .4066$**

Find  $P(z < -1.32)$



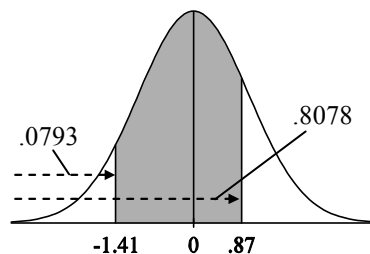
Read this *tail area* directly from the table.  
**Probability = .0934**

Find  $P(z \geq -1.32)$



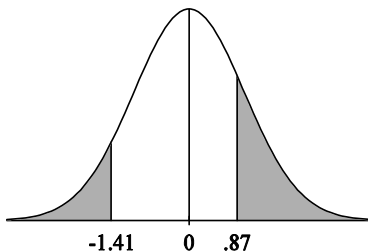
Even though the  $z$  score is negative, use the *cumulative* table with a positive  $z$ . Because of symmetry, you'll get the same area. (Or, subtract the *tail area* from 1.00)  
**Probability = .9066**

Find  $P(-1.41 \leq z \leq .87)$



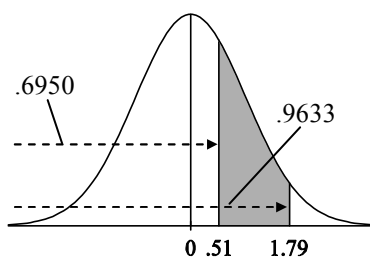
Look up the *cumulative* area for  $z = .87$ . Then subtract the *tail area* for  $z = -1.41$ .  
**Probability =  $.8078 - .0793 = .7285$**

**Find**  
 **$P(z \leq -1.41 \text{ or } z \geq .87)$**



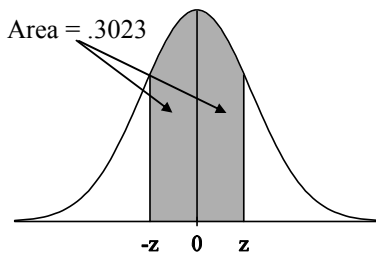
We already calculated the area between  $-1.41$  and  $.87$  to be  $.7285$ . Since the area under the entire curve equals  $1$ , just subtract  $.7285$  from  $1$  to find the combined area in the tails:  $1 - .7285 = .2715$ . (Or, find the *two tail areas* and add them:  $.0793 + .1922$ )  
**Probability = .2715**

**Find  $P(.51 \leq z \leq 1.79)$**



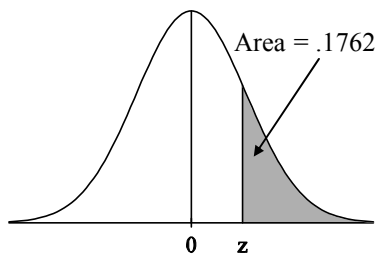
Find the *cumulative* area for  $z = 1.79$ . Then find the *cumulative* area for  $z = .51$  and subtract the smaller area from the larger area to get the area between  $.51$  and  $1.79$ .  
**Probability =  $.9633 - .6950 = .2683$**

**The area between  $z$  and  $-z$  is  $.6046$ .  
**Find  $z$ .****



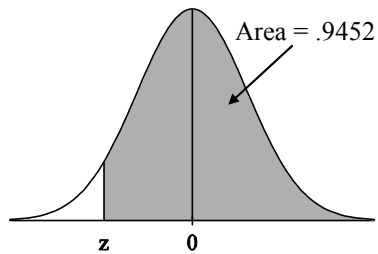
$z$  and  $-z$  are the same distance from zero (to the right and left). The area between them is  $.6046$ . Since they are the same distance from  $0$ , half of the  $.6046$  area is between each  $z$  and  $0$ . Add  $.5000$  to  $.3023$  and look up the area of  $.8023$  in the *cumulative* table – the corresponding  $z$  is  $.85$ .  
 **$z = .85$**

**The area to the right of  $z$  is  $.1762$ .  
**Find  $z$ .****



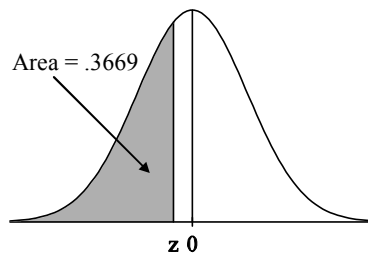
$1.0000 - .1762 = .8238$ , the *cumulative* area to the left of  $z$ . Look up this area – the corresponding  $z$  is  $.9300$ . Or, look up the area of  $.1762$  in the *tail-area* table and change the  $z$  score to positive.  
 **$z = .93$**

The area to the right of  $z$  is .9452.  
Find  $z$ .



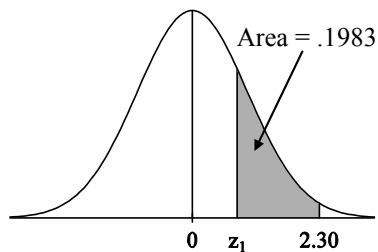
Since the area to the right of  $z$  is more than .5,  $z$  must lie to the left of 0. Look up .9452 in the cumulative table and change the  $z$  score to a negative. (Or, subtract .9452 from 1.000 and look up this tail area.) The corresponding  $z$  is -1.60.  
 **$z = -1.60$**

The area to the left of  $z$  is .3669.  
Find  $z$ .



The area to the left of  $z$  is less than .5, so  $z$  must be to the left of 0. Look up this area in the tail-area table – the corresponding  $z$  is -.34.  
 **$z = -.34$**

The area between  $z_1$  and  $z_0 = 2.30$  is .1983.  
Find  $z_1$ .



Look up the cumulative area for a  $z_0$  of 2.30 (= .9893). The area to the right of 2.3 is only .0107, so  $z_1$  must be to the left of 2.3 – between 0 and 2.3. Subtract .1983 from .9893 = .7910. Look up this area in the cumulative table – the corresponding  $z_1$  value is .81.  
 **$z_1 = .81$**